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Title

A generalization of the Cauchy-Riemann equations

The manifolds of constant rank defined by smooth equations

(1)
$$F_{n}(x_{1}, x_{2}, ..., x_{p}; t_{1}, t_{2}, ..., t_{q}) = 0$$

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involving parameters t_1, t_2, \dots, t_q are more general than the manifolds defined by atlases of maps. For such manifolds tangential derivatives exist for functions $\mathcal{U} = \mathcal{U}(x_1, \dots, x_p; t_1, \dots, t_q)$ which satisfy the equations

(2)
$$\frac{\partial u}{\partial t_{d}} = \sum_{\nu=1}^{N} \beta_{\nu} \frac{\partial F_{\nu}}{\partial t_{d}}, d = 1, ..., q.$$

As an example let (1) be the complex plane $x_1 - t_1 - it_2 = 0$ In this case the equations (2) turn into the Cauchy-Riemann equations.

For the functions satisfying (2) a generalized Cauchy integral formula holds.